

# Spatial Environmental Economics

## Lecture 5: Elements of Spatial Models

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# Roadmap

- ① Locations and the Topography of Space
- ② Spatial Links: Transportation
- ③ Spatial Forces
- ④ Summary

# Roadmap

① Locations and the Topography of Space

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# Locations

- A **location** is the geographic coordinates where economic activities take place
  - ▶ This could be a point in a map or an area
  - ▶ Definition will depend on the specific question(s) we want the model to answer
  - ▶ Definition can also depend on the available data
- The “topography” is the set of features of locations and their connections in space:
  - ▶ Productivities, amenities, spatial links
- More formally:
  - ▶ Define space  $S$ . **Locations**  $i \in S$
  - ▶ Productivities, amenities, spatial links are functions over locations  $i \in S$

# Productivity of locations

- Productivity of a location is the units of output per unit of associated labor used
  - ▶ It reveals the productive capacity of a location
  - ▶ It depends on the access to natural resources, climate, etc.
  - ▶ When there are more than one factors we refer to total factor productivity: the units of output for a unit of combined inputs
- Formally:
  - ▶ Denote the labor used in location  $i$  by  $L_i$
  - ▶ Then **productivity**  $A_i$  is the units of output per unit of labor  $L_i$
  - ▶ With a simple production function, output  $Y_i = A_i L_i$

# Amenity of locations

- Amenity of a location is the intrinsic utility value of residing there
  - ▶ It depends on access to entertainment, playgrounds, climate, water, etc
  - ▶ Diamond (2016) suggests six broad categories relevant for amenities:
    - ★ retail, transportation, crime, environmental, schooling, and job quality amenities
    - ★ e.g spending on parks per capita (positive), pollution (negative)
- Formally:
  - ▶ Denote the (indirect) utility of a location by  $W_i$
  - ▶ We can consider the **amenity**,  $u_i$ , such that  $W_i = W_i(w_i, P_i, u_i)$
  - ▶  $w_i$  is the wage,  $P_i$  is the price of consumption at the location

## Spatial links between locations

- Spatial links are the geographical connections between locations
  - ▶ They describe social links, economic links, and trade potential
  - ▶ Examples include trade, commuting, knowledge spillovers
- Spatial links across locations are determined by
  - ▶ The transportation and communication infrastructure
  - ▶ The means of transportation and communication

## Spatial links in the model

- We represent spatial links with a matrix (or a function in continuous space) with elements

$$\{\tau_{ij}\}_{i,j \in S}$$

- Each element of the matrix determines if two locations are directly linked
- The value (or the inverse) of each element represents the intensity of the link
  - ▶ E.g.  $i$  Munich,  $j$  Stuttgart,  $j'$  is Berlin: it is cheaper and faster to take a train to Stuttgart than Berlin so that  $\tau_{ij} < \tau_{ij'}$  where  $\tau_{ij}$  represents the cost of traveling from  $i$  to  $j$
  - ▶ We denote the cost of using each segment of the network as  $\bar{t}_{ij}$ , i.e. each  $\tau_{ij}$  is a function of  $\{\bar{t}_{ij}\}_{i,j \in S}$



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# Transportation infrastructure

- Transportation infrastructure is the network of installations that allows the transfers of goods through various means
  - ▶ Includes roads, rail tracks, airports, sea ports etc
  - ▶ It has significantly varied over time
  - ▶ Transportation revolutions correlate with significant economic and social progress
  - ▶ E.g. Persian empire, Ancient Athens/Hellenistic Period, Modern Roman Republic/Empire, Discovery of the New World, Industrial Revolution

# Telecommunication infrastructure

- Telecommunication infrastructure is the network of installations that allows the transfer of information through various means
- Includes information of any nature (signals, messages, pictures, voice etc) and by any means (wire, radio, optical, electromagnetic)

## Transportation technology

- The transportation technology also determines the intensity/quality of a link (and thus  $\bar{t}_{ij}$ )
- E.g. using donkey vs modern car vs plane
- Determines the speed or the type of objects that can be carried and as a result the overall cost,  $\tau_{ij}$

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# Spatial forces

- We have discussed the important elements of spatial economics
  - ▶ Productivities, amenities, transport costs
- Next: how to model some of the most significant economic forces that affect those
- We call these **spatial forces**:
  - ① Agglomeration
  - ② Amenity spillovers
  - ③ Transport congestion

# Agglomeration

- **Agglomeration** economies or agglomeration spillovers are the production increase as a result of clustering of economic activities
- Related to the idea that small scale production is inefficient because of fixed costs
- Externalities between firms in the same industry (Marshall, 1890) because of:
  - ▶ Labor market pulling
  - ▶ Knowledge spillovers
  - ▶ Proximity to inputs
- Externalities between firms in different industries (Jacobs)
  - ▶ E.g. R&D activity spillovers between disparate industries

## Agglomeration in our model

- Population/employment locally or elsewhere affects the productivity of a location  $i$ :

$$A_i = \bar{A}_i f^A(\{L_j\}_{j \in \mathcal{S}})$$

- ▶  $\bar{A}_i > 0$
  - ▶  $f^A$  is a function
  - ▶ If  $\partial A_i / \partial L_i > 0$  we say that there are *local* productivity spillovers
  - ▶ If  $\partial A_i / \partial L_j > 0$  for  $i \neq j$  we say that there are *spatial* productivity spillovers
- Simplest example:

$$A_i = \bar{A}_i L_i^\alpha$$

with  $\alpha \geq 0$



## Amenity spillovers

- **Amenity spillovers** or externalities occur if amenities are affected as a result of clustering of economic activities
- Variety of reasons underlying these spillovers, e.g.
  - ▶ Rental or housing market spillovers – more people wanting to live somewhere bid up prices
  - ▶ Air pollution from traffic, noise pollution from nightlife
  - ▶ Consumption amenities such as restaurants – need enough customers to cover fixed costs
  - ▶ Local public services such as schools or police force

## Amenity spillovers in our model

- Population/employment locally or elsewhere affects the amenity of a location  $i$ :

$$u_i = \bar{u}_i f^u \left( \{L_j\}_{j \in S} \right)$$

- ▶  $\bar{u}_i > 0$
  - ▶  $f^u$  is a function
  - ▶ If  $\partial u_i / \partial L_i \neq 0$  we say that there are *local* amenity spillovers
  - ▶ If  $\partial u_i / \partial L_j \neq 0$  for  $i \neq j$  we say that there are *spatial* amenity spillovers
- Simplest example:

$$u_i = \bar{u}_i L_i^{-\beta}$$

with  $\beta \neq 0$  (typically  $\beta > 0$ , congestion or dispersion force)

# Transport congestion

- **Transport congestion.** Congestion of the transportation system happens if the flows of goods or people or other endogenous variables affect the intensity/cost of the link
- In our model, we say that  $\tau_{ij}$  is a function of trade between two locations
  - ▶ As well as a function of the exogenous component  $\bar{t}_{ij}$ , as before

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# Basic elements of spatial models

- Locations:  $i \in S$
- Topography:  $A_i, u_i, \tau_{ij}$ 
  - ▶ Geography (economic fundamentals, exogenous):  $\bar{A}_i, \bar{u}_i, \bar{t}_{ij}$
  - ▶ Spatial forces: agglomeration ( $\alpha$ ), amenity spillovers ( $\beta$ ), transportation congestion
- Endogenous variables:  $L_i, w_i, P_i$

## Appendix

# References I

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